Constraints from the muon anomalous magnetic moment and $b \to s \gamma$ on gauge-mediated supersymmetry-breaking models

K.T. Mahanthappa and Sechul Oh

Department of Physics, University of Colorado, Boulder, CO 80309, USA E-mails: ktm@verb.colorado.edu, ohs@spot.colorado.edu

Abstract

We present a combined study of the muon anomalous magnetic moment, $a_{\mu} \equiv (g-2)_{\mu}/2$, and $b \to s\gamma$ decay in the minimal supersymmetric standard model with gauge-mediated supersymmetry-breaking. Combining new experimental data on a_{μ} and the branching ratio for $b \to s\gamma$, useful limits on the parameter space of these models are derived. Bounds on supersymmetric particle masses as a function of $\tan \beta$ are also presented.

1. Introduction

The gauge-mediated supersymmetry breaking (GMSB) models have been of special interest, because they have attractive features of natural suppression of the supersymmetry (SUSY) contributions to flavor-changing neutral currents at low energies and prediction of the supersymmetric particle mass spectrum in terms of few parameters.

The decay process $b \to s \gamma$ does not occur at the tree level, and at one-loop level it occurs at a small rate but enough to be sensitive to effects of new physics. The CLEO collaboration has recently reported the branching ratio for the decay $b \to s \gamma$ [1]: $2.0 \times 10^{-4} < \mathrm{BR}(b \to s \gamma) < 4.5 \times 10^{-4}$ at 95 % C.L. The anomalous magnetic moment of muon, $a_{\mu} \equiv (g-2)_{\mu}/2$, is also sensitive to new physics effects and can be used to constrain SUSY models [2, 3], on account of the great accuracy of both experimental and the standard model (SM) theoretical values of a_{μ} . The present experimental value of a_{μ} [4] is $a_{\mu}^{\rm exp} = 11659230(84) \times 10^{-10}$, while the theoretical prediction for a_{μ} in the context of the SM is $a_{\mu}^{\rm SM} = 11659162(6.5) \times 10^{-10}$ [2].

In this work, we obtain combined constraints due to both $b \to s\gamma$ decay and a_{μ} in the minimal supersymmetric SM (MSSM) with GMSB. Even though there exist the previous works which studied either $b \to s\gamma$ [2, 5] or a_{μ} [3] in the GMSB models, our work extends the previous ones in the sense that we investigate both $b \to s\gamma$ and a_{μ} together with the inclusion of the supersymmetric one-loop

correction to the mass of b quark, m_b , which has considerable effects in large $\tan \beta$ region as we see below. Furthermore, in this combined study, we explicitly show that, with the presently available experimental data, constraints from the decay $b \rightarrow s \gamma$ are more stringent than those from a_{μ} in broad region of the parameter space.

2. The model

In the GMSB models messenger fields transmit SUSY breaking to the fields of visible sector via loop diagrams involving $SU(3)_C \times SU(2)_L \times U(1)_Y$ gauge interactions.

The radiatively generated soft SUSY-breaking masses of gauginos and scalars at messenger scale M are given in terms of $\Lambda = F/M$ (\sqrt{F} is the original SUSY-breaking scale), the SM gauge couplings α_i (i=1,2,3) and the effective number of messenger fields n [$n=n_5+3n_{10}$, where n_5 and n_{10} denote the number of $(\mathbf{5}+\bar{\mathbf{5}})$ and $(\mathbf{10}+\overline{\mathbf{10}})$ pairs, respectively]. It is known that for messenger fields in complete SU(5) representation, at most four $(\mathbf{5}+\bar{\mathbf{5}})$ pairs, or one $(\mathbf{5}+\bar{\mathbf{5}})$ and one $(\mathbf{10}+\overline{\mathbf{10}})$ pair are allowed to ensure that the gauge couplings remain perturbative up to the GUT scale.

3. The analysis

We require that electroweak symmetry be radiatively broken. The parameter Λ is taken to be around 100 TeV to ensure that the sparticle masses

are of the order of the weak scale. The case $M = \Lambda$ is excluded since it produces a massless scalar in the messenger sector. The upper bound on the gravitino mass of about 10^4 eV restricts $M/\Lambda < 10^4$. In running the renormalization group equations, we include the one-loop correction to the running bottom quark mass, Δm_b , which involves the contributions coming from gluino-sbottom loop diagram and chargino-stop loop diagram.

In $b \to s \gamma$ decay, the contributions to the total decay amplitude are coming from the W loop diagram, charged Higgs boson loop diagram, neutralino loop diagram, and gluino loop diagram. It has been pointed out that the neutralino and gluino contributions to the amplitude are less than 1 % in the whole range of parameter space [5]. The charged Higgs boson loop contribution adds constructively to the W loop contribution, while the chargino loop contribution can be constructive or destructive to the W loop contribution, but is generally much smaller than the charged Higgs boson loop contribution.

The supersymmetric contributions, δa_{μ}^{SUSY} , to the muon anomalous magnetic moment are essentially coming from neutralino-smuon loop diagram and chargino-sneutrino loop diagram. The bound on the supersymmetric contributions to a_μ is given by -71×10^{-10} < $\delta a_\mu^{\rm SUSY}$ < $207\times$ 10^{-10} at 90 % C.L. This bound is obtained by the difference between experimental value and theoretical prediction of a_{μ} . The new E821 experiment at Brookhaven is expected to improve the experimental determination of a_{μ} to the level of 4×10^{-10} [6]. The electroweak contribution to a_{μ} in the SM up to two-loops is $a_{\mu}^{\rm EW}=15.1(0.4)\times 10^{-10}$. Any deviation from this value in the new E821 experiment could be attributed to SUSY as its contribution could be as large or larger than this value [2].

We use our calculated mass spectrum and couplings to calculate the rate for $b \to s\gamma$ and $\delta a_{\mu}^{\rm SUSY}$. The results depend on physical variables $\tan \beta$, $|\mu|$, ${\rm sign}(\mu)$, M/Λ , and n. Our results for both the branching ratio for $b \to s\gamma$ and $\delta a_{\mu}^{\rm SUSY}$ are presented as a function of the weak gaugino mass M_2 , $|\mu|$, for fixed values of $\tan \beta$, n and ${\rm sign}(\mu)$. M_2 is directly related to Λ . Then the bounds on the branching ratio for $b \to s\gamma$ and $\delta a_{\mu}^{\rm SUSY}$ are translated into the bounds on values of M_2 and $|\mu|$ in the $|\mu|-M_2$ plane for fixed values of $\tan \beta$, n and ${\rm sign}(\mu)$. Bounds on other sparticle masses can be easily deduced from a bound on M_2 .

In Figs. 1–3, we display the bounds obtained from the branching ratio for $b \to s \gamma$ and $\delta a_{\mu}^{\rm SUSY}$ in the $|\mu| - M_2$ plane for n = 1 and either sign of μ , for

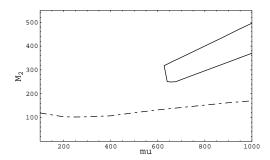


Figure 1. Limits on the weak gaugino mass M_2 as a function of $|\mu|$ for $\tan \beta = 10$, $\mu > 0$ and n = 1. Units are in GeV. Solid lines represent the bounds from the branching ratio for $b \to s\gamma$ (the region surrounded by the solid line is allowed) and dot-dashed lines represent the lower bounds from a_{μ} .

each of the values of $\tan\beta=10$ and 60. Solid lines represent the bounds from the branching ratio for $b\to s\gamma$ and dot-dashed lines describe the bounds from $\delta a_\mu^{\rm SUSY}$.

Figs. 1 and 2 show the bounds on M_2 and $|\mu|$ for $\tan \beta = 10$ and n = 1, and for positive and negative μ , respectively. The region surrounded by the solid line is allowed by the CLEO bound, while the upper region of the dot-dashed line is allowed by the present bound on a_{μ} . In the case of Fig. 1, the constraint from $b \to s\gamma$ decay is clearly much stronger than that from a_{μ} . We find $M_2>248$ GeV and $\mu>626$ GeV. Small values of M_2 lead to unacceptably large contribution to the branching ratio for $b \to s\gamma$, while large values of μ raise the problem of fine-tuning and are generally constrained by the lower bound on the stau mass. In Fig. 2 we see the constrains from both $b \to s\gamma$ and a_{μ} are complementary. By combining the bounds from the both, we can obtain much stronger bound on M_2 and $|\mu|$; in particular, low values of $|\mu|$ which would have been allowed are excluded. We find $M_2 > 210$ GeV and $|\mu| > 505$ GeV.

In large $\tan \beta$ case, we find that the bound from either $b \to s \gamma$ or a_{μ} is more stringent than that in small $\tan \beta$ case, and most region in the $|\mu| - M_2$ plane is excluded. For $\tan \beta = 60$ and $\mu > 0$ (Fig. 3), the allowed regions from each of $b \to s \gamma$ and a_{μ} do not overlap, even though a possibility exists that they might overlap for unacceptably very large values of μ . Thus, this case is excluded, while it would be allowed if one considered only either $b \to s \gamma$ or a_{μ} as in Refs. [3,5]. For $\tan \beta \lesssim 50$ and $\mu > 0$, the allowed regions from each of $b \to s \gamma$ and a_{μ} overlap allowing limited regions in the parameter space. For $\tan \beta = 60$ and $\mu < 0$,

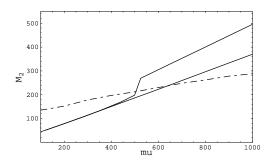


Figure 2. The same as Fig. 1, except $\mu < 0$.

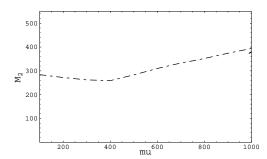


Figure 3. The same as Fig. 1, except $\tan \beta = 60$.

the supersymmetric one-loop correction to bottom quark mass leads to unacceptably large value of m_b , unless one makes additional assumptions like $b-\tau$ Yukawa coupling unification [2]. To keep our analysis in a general form in the context of the GMSB models, we adopt no further assumptions like $b-\tau$ unification. Thus, by inclusion of the correction Δm_b , we exclude the case of large $\tan \beta$ and $\mu < 0$. For n = 3 [2], large $\tan \beta$ region is almost ruled out due to the same reason as the case of n = 1.

In Fig. 4 we plot the bounds on the sparticle masses, obtained by this combined analysis of $b \to s\gamma$ and a_{μ} , as a function of $\tan \beta$ for positive μ and n=1. The plots are displayed for up to $\tan \beta \approx 50$, since the region corresponding to $\tan \beta \gtrsim 50$ is ruled out. The lower bounds on the sparticle masses increase monotonically as $\tan \beta$ does. For n=3, the lower bound on each sparticle mass is higher than that for n=1.

4. Conclusion

In our analysis, the large $\tan \beta$ region is ruled out or severely constrained, depending on the sign of μ . By inclusion of the supersymmetric one-loop correction to b quark mass, we have found

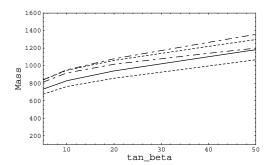


Figure 4. Bounds on the sparticle masses (in GeV) as a function of $\tan \beta$ for $\mu > 0$ and n = 1. The solid line represents the lower bound on the gluino mass, and the dotted and dot-dashed lines represent the lower bounds on the stop $(m_{\tilde{t}_1} \text{ and } m_{\tilde{t}_2})$ and sbottom $(m_{\tilde{b}_1} \text{ and } m_{\tilde{b}_2})$ masses, respectively.

that the region of large $\tan \beta$ and negative μ is physically ruled out in order to give a correct value of m_b , unless one makes further assumptions such as $b - \tau$ Yukawa coupling unification. With the present experimental data for $b \rightarrow s\gamma$ and a_{μ} , constraints from the decay $b \rightarrow s\gamma$ are more stringent than those from a_{μ} in broad region of the parameter space. However, if the Brookhaven E821 experiment approaches the expected precision of the level of 4×10^{-10} in determination of a_{μ} in near future, constraints from a_{μ} are expected to become much more stringent than the present ones. We could anticipate more severe constraints on the parameter space with the future precise measurements of the branching ratio of $b \to s\gamma$ and a_{μ} .

This work was supported in part by the US Department of Energy Grant No. DE FG03-95ER40894.

References

- [1] Ahmed S et al, CLEO collaboration 1999 CLEO CONF 99-10, hep-ex/9908022.
- Mahanthappa K.T and Oh S 1999 COLO-HEP-434, hep-ph/9908531, and references therein.
- [3] Carena M, Giudice G.F, and Wagner C.E.M 1997 Phys. Lett. B 390 234.
- [4] Particle Data Group: Review of Particle Physics 1998 Euro. Phys. J. C 3 280.
- [5] Deshpande N.G, Dutta B, and Oh S 1997 Phys. Rev. D 56 519.
- [6] Carey R.M et al 1999 Phys. Rev. Lett. 82 1632.